

## 2. Generation of random numbers (rejection method)

**Task 1.** /5 points/ Apply rejection method to generate random numbers with p.d.f.  $f()$  using supporting p.d.f.  $g()$  and constant  $c$ :

No	Distribution names	p.d.f. $f(x)$	p.d.f. $g(x)$	$c$
1	$f$ -normal $N(0,1)$ $g$ -Laplace	$f(x) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{x^2}{2}\right)$	$g(x) = \frac{1}{2} \exp(- x )$	$c = \sqrt{\frac{2e}{\pi}}$
2	$f$ -Beta(2,1) $g$ -uniform $U[0,1]$	$f(x) = \frac{\Gamma(2+1)}{\Gamma(2)\Gamma(1)} x^1 (1-x)^0 \mathbf{1}\{0 \leq x \leq 1\}$	$g(x) = \mathbf{1}\{0 \leq x \leq 1\}$	$c = 2$
3	$f$ -Beta(3,2) $g$ -uniform $U[0,1]$	$f(x) = \frac{\Gamma(3+2)}{\Gamma(3)\Gamma(2)} x^2 (1-x)^1 \mathbf{1}\{0 \leq x \leq 1\}$	$g(x) = \mathbf{1}\{0 \leq x \leq 1\}$	$c = \frac{16}{9}$
4	$f$ -Beta(3/2,3/2) $g$ -uniform $U[0,1]$	$f(x) = \frac{\Gamma(3)}{\Gamma(3/2)\Gamma(3/2)} x^{\frac{1}{2}} (1-x)^{\frac{1}{2}} \mathbf{1}\{0 \leq x \leq 1\}$	$g(x) = \mathbf{1}\{0 \leq x \leq 1\}$	$c = \frac{1}{\Gamma(3/2)^2} = \frac{4}{\pi}$
5	$f$ -triangular $g$ -uniform $U[0,1]$	$f(x) = 2(1-x) \mathbf{1}\{0 \leq x \leq 1\}$	$g(x) = \mathbf{1}\{0 \leq x \leq 1\}$	$c = 2$

Rejection method:

1. Generate  $u \sim U[0, 1]$ .
2. Generate  $x$  having the p.d.f.  $g(x)$ .
3. Create the pairs  $(x, y) = (x, cg(x)u)$  for  $c = \max \frac{f(x)}{g(x)}$ .
4. Reject the pairs  $(x, y)$  that do not fulfill the condition  $cg(x)u \leq f(x)$ .

Plot histograms for generated data. Plot theoretical probability density functions - see `pdf` function in MATLAB.

/Total: 5 points/